## EML 5526

FINITE ELEMENT ANALYSIS \& APPLICATIONS

Instructor: Nam-Ho Kim, Raphael T. Haftka
Class hour: 12:50-1:40 PM, MWF
Class room: 102 NEB
Office: 210 MAE-A
Office hour: MWF $5^{\text {th }}$ period (11:45-12:35)
Phone: 352-846-0665
E-mail: nkim@ufl.edu
http://www.mae.ufl.edu/nkim/eml5526/

## SYLLABUS

- Teaching Assistants
- Mr. Vijay Jagdale
- Office: 235 NEB, Phone: 392-2524
- Office hour: TTh $4^{\text {th }}$ period (10:40-11:30), e-mail: vjagdale@ufl.edu
- Textbooks:
- Concepts and Applications of Finite Element Analysis $4^{\text {th }}$ Ed, by R. D Cook, D. S. Malkus, M. E. Plesha, R. J. Witt, Wiley, 2002
- Required.
- Software:
- Projects and some HWs will require FE software Abaqus
- Download and install from http://campus.3ds.com/simulia/freese
- Must use your personal computer, not lab computers

OFFICE HOURS

| Period | Mon | Tue | Wed | Thu | Fri |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $7: 25-8: 15$ |  |  |  |  |  |
| $8: 30-9: 20$ |  |  |  |  |  |
| $9: 35-10: 25$ |  |  |  |  |  |
| 10:40-11:30 |  | TA Vijay |  | TA Vijay |  |
| 11:45-12:35 | Office hour |  | Office hour |  | Office hour |
| 12:50-1:40 | EML5526 |  | EML5526 |  | EML5526 |
| $1: 55-2: 45$ |  |  |  |  |  |
| 3:00-3:50 |  |  |  |  |  |
| $4: 05-4: 55$ |  |  |  |  |  |

Instructor: Nam Ho Kim, 210 MAEA, 846-0665, nkim@ufl.edu
Instructor: Raphael T. Haftka, 220 MAEA, 392-9595, haftka@ufl.edu
Vijay Jagdale: 235 NEB, 392-2524, vjagdale@ufl.edu
Class Website: http://www.mae.ufl.edu/nkim/eml5526.htm|
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## GRADES

- Homework
- All assigned homeworks must be submitted before starting the due date class. Solution will be posted on the class website. No late homeworks will be accepted.
- Exams
- Two, equally contributing examinations
- Tentative schedules: Feb. 24 (Exam1), Apr. 21 (Exam2)
- Quiz: There will be quizzes during the class


## - Projects

- Two projects in finite element analysis using Abaqus. Formal report is required. $10 \%$ penalty for late submission and no acceptance after one week. $\qquad$
- Grading
- Exams (40\%), Projects (40\%), Homework+Quiz (20\%) $\qquad$
$\qquad$

| COURSE SCHEDULES COnt. |  |  |
| :--- | :--- | :--- |
| Date | Class | Reading Assignment |
| $1 / 6 \mathrm{~W}$ | Introduction to finite element analysis | Chapter 1 |
| $1 / 8 \mathrm{~F}$ | 1-D Bar element, assembly, applying BC | $2.1,2.2,2.5,2.7$ |
| $1 / 11 \mathrm{M}$ | Stress, strain, stifness matrix, plane truss | $2.4,2.6$ |
| $1 / 13 \mathrm{~W}$ | Space truss, sparsity, Mechanical load, stress | $2.8,2.9$ |
| $1 / 15 \mathrm{~F}$ | Thermal strain, stress; modeling symmetry | $2.10,2.11$ |
| $1 / 18 \mathrm{M}$ | M. L. King Holiday, No class |  |
| $1 / 20 \mathrm{~W}$ | Introduction to Abaqus |  |
| $1 / 22 \mathrm{~F}$ | Beam theory | $2.3,4.1,4.2$ |
| $1 / 25 \mathrm{M}$ | Potential energy | $4.3,4.4$ |
| $1 / 27 \mathrm{~W}$ | Rayleigh-Ritz method, FE interpolation | $4.5,4.6$ |
| $1 / 29 \mathrm{~F}$ | FE equation for beam, distributed load | 4.8 |
| $2 / 1 \mathrm{M}$ | Plane frame, convergence | 4.9 |
| $2 / 3 \mathrm{~W}$ | FE analysis of beam using Abaqus |  |
| $2 / 5 \mathrm{~F}$ | CST, LST elements | $3.1,3.2,3.3,3.4,3.5$ |
| $2 / 8 \mathrm{M}$ | Q4, Q8, Q9 elements | $3.6,3.7$ |
| $2 / 10 \mathrm{~W}$ | Project 1 assignment |  |
| $2 / 12 \mathrm{~F}$ | Numerical integration | 3.9 |

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

| COURSE SCHEDULES cont. |  |  |
| :---: | :---: | :---: |
| Date | Class | Reading Assignment |
| 2/15 M | Drilling DOF, incompatible modes, reduced integration | 3.10, 3.11 |
| 2/17 W | Stress calculation | 3.12 |
| 2/19 F | FE analysis of stress concentration |  |
| 2/22 M | Review of exam |  |
| $2 / 24$ W | First In term exam |  |
| 2/26 F | Galerkin Method in one dimension | 5.1,5.3 |
| 3/1 M | Galerkin Method in 2 D and mixed formulations | 5.5, 5.6. |
| $3 / 3 \mathrm{~W}$ | Review of formulation techniques. | Project 1 due |
| 3/5 F | Isoparametric elements | 6.1,6.2 |
| $3 / 8 \mathrm{M}$ | Spring break, no class |  |
| 3/10 W | Spring break, no class |  |
| 3/12 F | Spring break, no class |  |
| 3/15 M | Quadrature and Q8,Q9 elements | 6.3, 6.4 |
| 3/17 W | Incompatible modes, and static condensation | 6.6, 6.7 |
| 3/19 F | Stress calculations | 6.10, 6.11 |
| 3/22 M | Validity of isoparameteric elements and patch test | 6.11, 6.12. |
| $3 / 24 \mathrm{~W}$ | Review of Chapter 6. |  |


| COURSE SCHEDULES cont. |  |  |
| :--- | :--- | :--- |
| Date | Class | Reading Assignment |
| $3 / 26 \mathrm{~F}$ | Isoparametric triangles and tetrahedral | $7.1,7.2$ |
| $3 / 29 \mathrm{M}$ | Coordinate transformation | $8.1,8.2,8.3$ |
| $3 / 31 \mathrm{~W}$ | Connecting dissimilar elements and fracture mechanics | $8.5,8.7$ |
| $4 / 2 \mathrm{~F}$ | Reanalysis. | 8.9 |
| $4 / 5 \mathrm{M}$ | III-conditioning and the condition number | $9.1-9.3$ |
| $4 / 7 \mathrm{~W}$ | Decay test, residual and convergence rate | $9.4-9.6$ |
| $4 / 9 \mathrm{~F}$ | Multi-mesh extrapolation | 9.7 |
| $4 / 12 \mathrm{M}$ | Mesh revision and gradient recovery | $9.8,9.9$ |
| $4 / 14 \mathrm{~W}$ | Adaptive meshing | $9.9,9.11$ |
| $4 / 16 \mathrm{~F}$ | Review of Chapter 9 |  |
| $4 / 19 \mathrm{M}$ | Review for second in-term exam. |  |
| $4 / 21 \mathrm{~W}$ | Second in-term exam. |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |

## TIPS FOR A

- Be patient and persistent
- Read the text repeatedly until you understand it.
- If you don't understand it, ask a question until you get answered. $\qquad$
- Follow equations
- Do not just read the equation.
- You must follow all equations by HAND, not EYE.
- Try to understand the meaning of equations
- If you memorize an equation that you don't understand, you can't solve the problem. Math is a language.
- Follow the instruction carefully
- Read carefully what is asked. If $A$ is asked, then answer $A$ not $B$.
- Do not submit a blank answer. $\qquad$


## INTRODUCTION TO FINITE ELEMENT METHOD

- What is the finite element method (FEM)?
- A technique for obtaining approximate solutions to boundary value problems.
- Partition of the domain into a set of simple shapes (element)
- Approximate the solution using piecewise polynomials within the element

$$
\left\{\begin{array}{l}
\frac{\partial \sigma_{x x}}{\partial x}+\frac{\partial \tau_{x y}}{\partial y}+b_{x}=0 \\
\frac{\partial \tau_{x y}}{\partial x}+\frac{\partial \sigma_{y y}}{\partial y}+b_{y}=0
\end{array}\right.
$$



## INTRODUCTION TO FEM cont.

- How to discretize the domain?
- Using simple shapes (element)
$\circ-$

- All elements are connected using "nodes".

- Solution at Element 1 is described using the values at Nodes 1, 2, 6, and 5 (Interpolation).
- Elements 1 and 2 share the solution at Nodes 2 and 6.


## INTRODUCTION TO FEM cont.

- Finite element analysis solves for Nodal Solutions
- All others can be calculated (or interpolated) from nodal solutions

- Displacement within the element

$$
u(x)=a+b x=u_{1}+\frac{u_{2}-u_{1}}{L} x=\left(\frac{L-x}{L} u_{1}+\left(\frac{x}{L} u_{2}\right.\right.
$$

- Strain of the element

Interpolation (Shape) Function

$$
\varepsilon(x)=\frac{\partial u}{\partial x}=-\frac{1}{L} u_{1}+\frac{1}{L} u_{2}
$$

$\qquad$

## INTRODUCTION TO FEM cont.

- How to calculate nodal solutions?

Construct a huge simultaneous system of equations and solve for nodal solutions.

- Different physical problems have different matrices and vectors.

$$
\left[\begin{array}{cccc}
K_{11} & K_{12} & \cdots & K_{1 n} \\
K_{21} & K_{22} & \cdots & K_{2 n} \\
\vdots & \vdots & \ddots & \vdots \\
K_{n 1} & K_{n 2} & \cdots & K_{n n}
\end{array}\right]\left\{\begin{array}{c}
u_{1} \\
u_{2} \\
\vdots \\
u_{n}
\end{array}\right\}=\left\{\begin{array}{c}
F_{1} \\
F_{2} \\
\vdots \\
F_{n}
\end{array}\right\}
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## EXAMPLE: FINITE ELEMENTS

- Plastic Wheel Cover Model
- 30,595 Nodes, 22,811 Elements
- Matrix size is larger than $150,000 \times 150,000$.
- MSC/PATRAN (Graphic user interface)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

EXAMPLE: AIRBAG DEPLOYMENT

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


