## Principles of Engineering Analysis I & II EGM 6321 & 6322

Instructor Dr. Thomas L Jackson

Office	205B Particle Science and Technology Building
Email	<u>tlj@ufl.edu</u>
Credit	Three hours
Spring Term:	
Time	Tuesday 1:55 – 2:45 pm
	Thursday 1:55 – 3:50 pm
Location	CSE E122
Office Hours	M 2:30 – 4 pm
	Tu 3 – 4 pm

**Grading:** Homework will be assigned regularly and due at the beginning of class. Only selected homework problems will be graded, and at random.

**Honor Code:** It is assumed that the Florida Student Code will be followed at all times, including during completion of homework and during exams.

## **Suggested books**

- 1. Butkov, *Mathematical Physics*, (1968).
- 2. Churchill and Brown, *Complex Variables and Applications*, 5th Edition, (1990).
- Boyce and DiPrima, <u>Elementary Differential Equations and Boundary Value Problems</u>, 4<sup>th</sup> Edition, (1986).
- 4. Drazin, Nonlinear Systems, (1992).
- 5. Churchill and Brown, *Fourier Series and Boundary Value Problems*, 4th Edition, (1987).
- 6. Churchill, *Operational Mathematics*, (1972).
- 7. Haberman, *Elementary Applied Partial Differential Equations*, 2<sup>nd</sup> Edition, (1987).
- 8. Dennemeyer, *Introduction to Partial Differential Equations and Boundary Value Problems*, (1968).
- 9. Greenberg, *Foundations of Applied Mathematics*, (1978).

## Course Outline for EGM 6321 and 6322

- 1. Complex Variables Churchill and Brown, 5th Edition, 1990
  - a. Complex numbers definition, algebraic properties, geometric interpretation, triangle inequality, polar form, exponential form, Euler's formula, powers and roots (Chapter 1)
  - b. Analytic functions mappings, derivative, Cauchy-Riemann equations, analytic functions, singular point, harmonic functions (Chapter 2)
  - c. Elementary functions exponential, trigonometric, hyperbolic, logarithmic and its branches, Riemann surfaces (Chapter 3)
  - d. Integration basic rules, contour integration, Cauchy-Goursat Theorem, simply and multiply connected domains, Cauchy Integral Formula (Chapter 4)
  - e. Residues Laurent series, residues, Residue Theorem, residues at poles, improper real integrals, Cauchy Principal Value, Inverse Laplace Transform, Jordan's inequality (Chapters 5 and 6; Butkov, 1968, Chapter 2)
  - f. Application of complex variables to two-dimensional potential flows
- 2. Ordinary Differential Equations (ODE)
  - Brief Review classification, 1<sup>st</sup> order equations, 2<sup>nd</sup> order linear equations, Wronskian, constant coefficient, nonhomogeneous problems (Boyce and DiPrima, 4<sup>th</sup> Edition, 1986, Chapters 1-3)
  - b. Second order linear ODE variable coefficients, singular points, Fuchs' Theorem, Frobenius method (Butkov, 1966, Chapter 3)
  - c. First order systems
    - i. Linear systems brief review, eigenvalues, eigenvectors, Wronskian, trajectories (Boyce and DiPrima, 4<sup>th</sup> Edition, 1986, Chapter 7)
    - Nonlinear systems autonomous systems, phase plane, critical points, trajectories, almost linear systems, direct method of Liapaunov (Boyce and DiPrima, 4<sup>th</sup> Edition, 1986, Chapter 9; Drazin, 1992, Chapter 6)
    - iii. Introduction to bifurcation theory stability, turning point, transcritical bifurcation, pitchfork bifurcation, Hopf bifurcation (Drazin, 1992, Chapter 1)
- 3. Fourier Series
  - a. Orthogonal functions (Churchill and Brown, 4<sup>th</sup> Edition, 1987, Chapter 5)
  - b. Fourier expansion, Fourier cosine series, Fourier sine series, complex form (Butkov, 1968, Chapter 4; see also Churchill and Brown, 4<sup>th</sup> Edition, 1987, Chapters 3-5)
- 4. Laplace Transform
  - a. General linear integral transformations, Laplace transforms, inverse Laplace transform, properties of Laplace transforms, Dirac delta function, convolution, properties of convolution, application to PDEs (Churchill, 1972, Chapters 1-3; see also Butkov, 1968, Chapter 5)
- 5. Fourier Transform
  - a. Discrete and continuous spectrum, Fourier transform, properties, convolution, Fourier Integral Theorem, Fourier sine and cosine transforms, application to PDEs (Butkov, 1968, Chapter 7; see also Churchill, 1972, Chapters 11-13)

- 6. Partial Differential Equations (PDE)
  - a. Classification
  - b. Methods for solving hyperbolic, parabolic, and elliptic PDEs, Separation of Variables
  - c. Strum-Liouville eigenvalue problems
  - d. Method of characteristics, expansions waves, shocks, Whitman's equal-area principle
  - e. Haberman, 2<sup>nd</sup> Edition, (1987); Dennemeyer (1968)
- 7. Green's Functions
- 8. Variational Methods
- 9. Perturbation Methods